

On Round-Optimal Zero Knowledge in the Bare Public Key Model

Alessandra Scafuro and Ivan Visconti
University of Salerno
ITALY

FOCUS: Round-Optimal (4 rounds)
concurrent and resettable Zero Knowledge
in the Bare Public Key Model

have already been achieved:

Round-optimal Concurrent ZK:
(standard assumptions)

- [Z03] only sequential soundness,
- [DV05] concurrent soundness,
- [V06] efficiently,
- [D09] minimal assumptions,
- [YZ10] sophisticated notion of argument of knowledge.

Round-optimal Resettable ZK:
(complexity leveraging)

- [MR01] only sequential soundness,
- [DPV04] concurrent soundness,
- [YZ07] under generic assumptions.

What do we do in this paper ?

Our Contribution

- ✦ Point-out a subtle issue in the zero knowledge proof of *all round-optimal* (concurrent and resettable) protocols.

Alternative proof?

Protocol's structure of almost all round-optimal protocols makes problematic the design of any simulator.

Exceptions: *could* admit alternative simulators:

- Resettable ZK of [YZ07]: uses complexity leveraging.
- Concurrent ZK of [Z03]: only sequential soundness.

- ✦ New round-optimal concurrent ZK with concurrent soundness and standard assumptions.

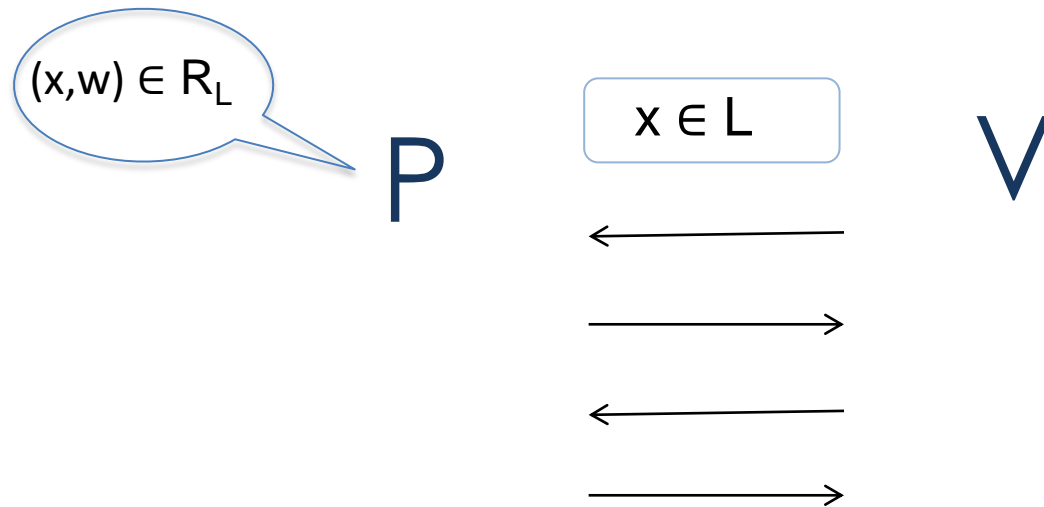
- The same protocol admits efficient implementation.
- Round-optimal resettable ZK (similar to [YZ07]), with a new proof.

Outline

- Definitions
 - Concurrent Zero Knowledge
 - Bare Public Key (BPK) Model
 - Concurrent Zero Knowledge and Soundness in the BPK model
- Round-optimal Concurrent Zero Knowledge:
 - the issue of *all* zero-knowledge simulators
 - the difficulty of designing any alternative simulator
- Our technique

Zero knowledge Interactive Proofs

(standard model)



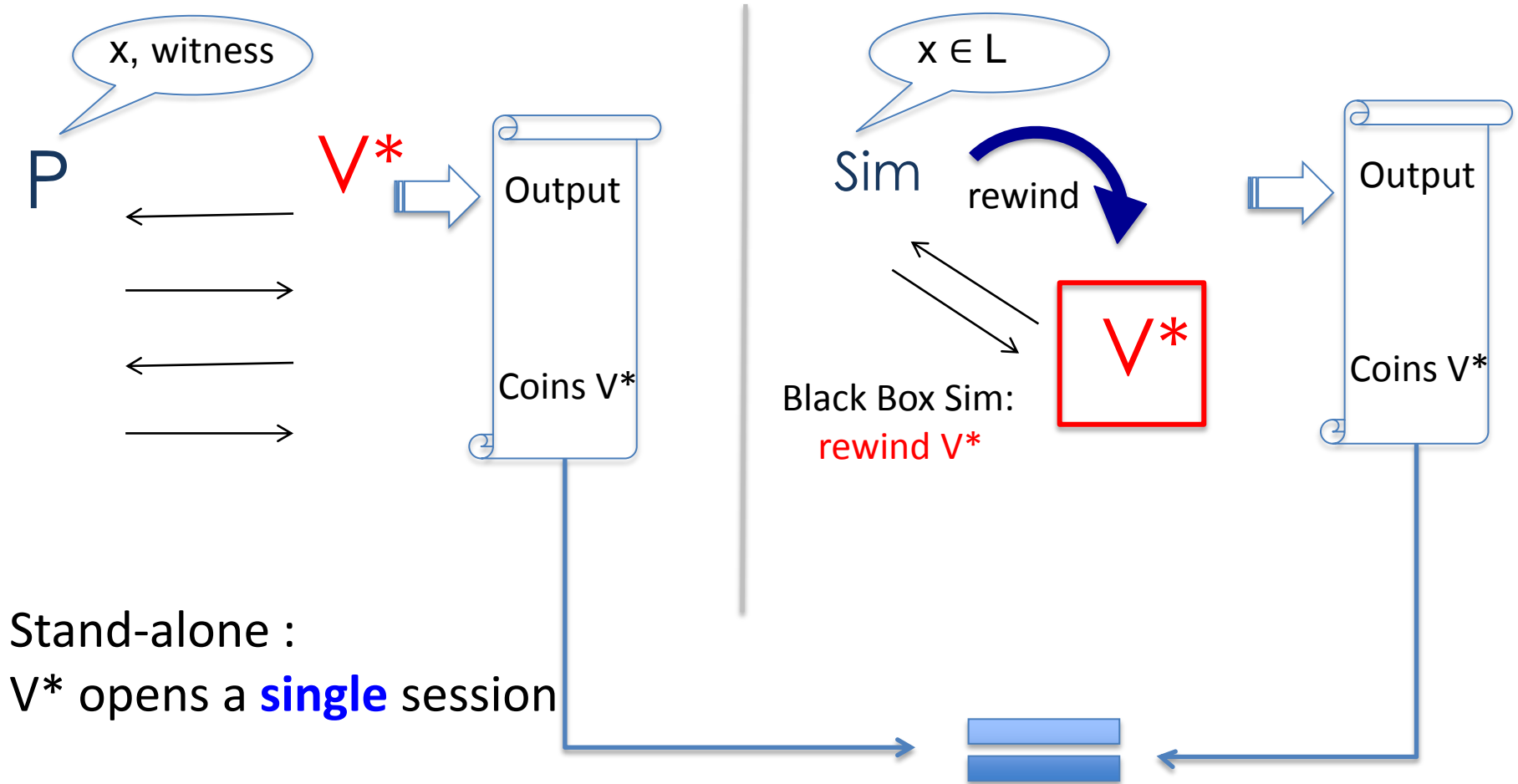
Completeness: if both P and V are honest, V accepts the proof.

Soundness: if the theorem is false any P^* cannot convince V .

Zero Knowledge: (intuition) any V^* learns nothing but the fact that the theorem is true.

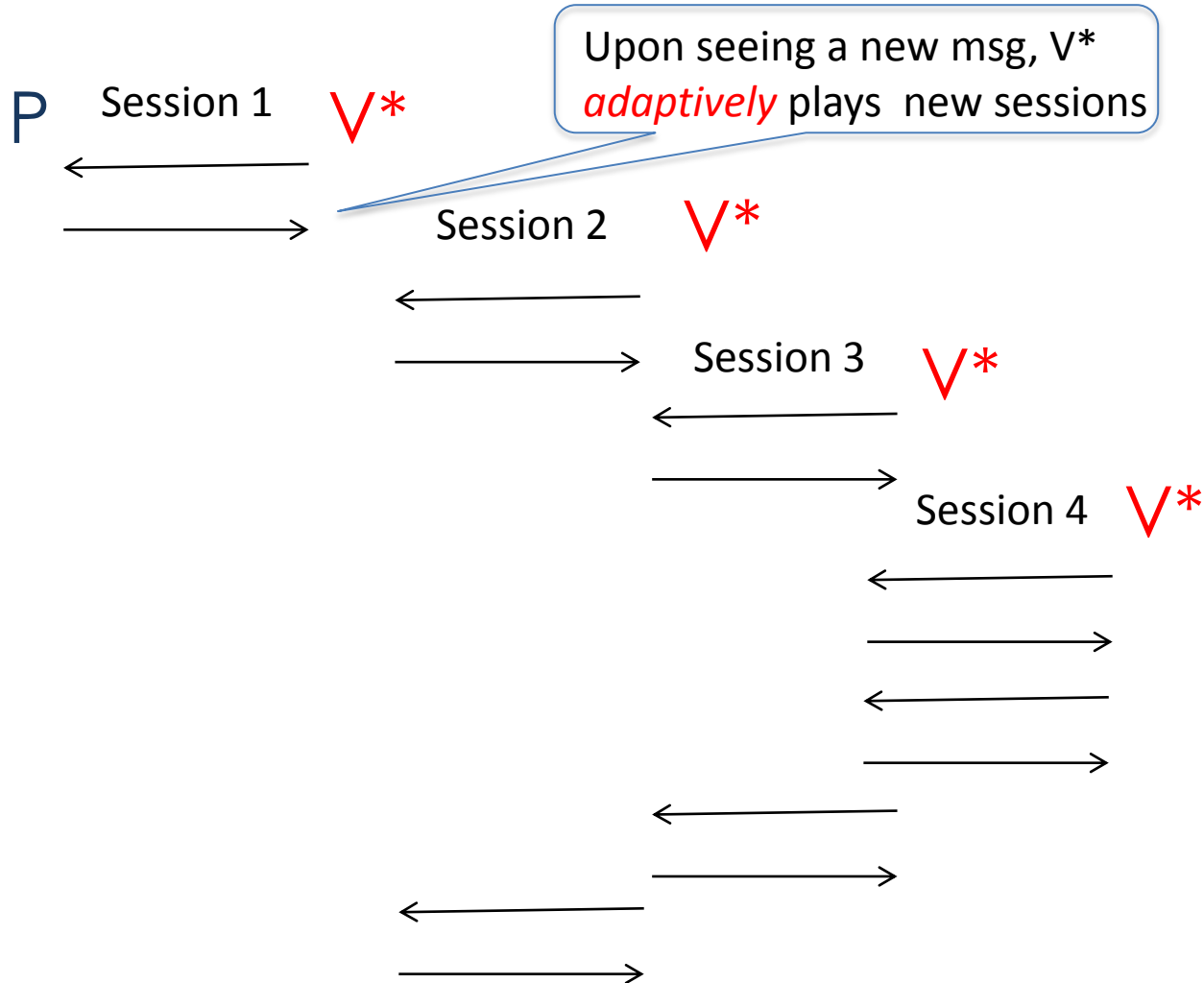
Zero Knowledge (stand-alone)

V^* does not learn anything?



Concurrent Zero Knowledge

More realistic setting: V^* can open *many sessions concurrently*.



Constant-round concurrent black-box Zero Knowledge (cZK) in the standard model is **impossible** [CKPR01].

Achieving black-box constant-round cZK *requires setup assumptions.*

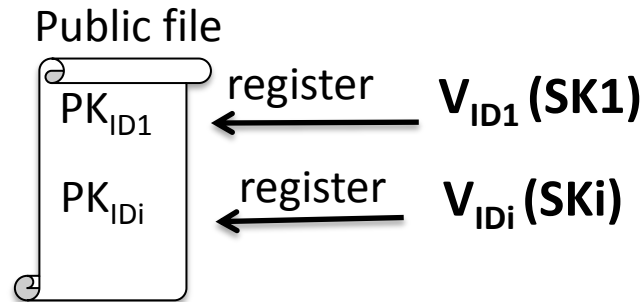
Bare Public Key Model

Introduced in STOC 2000 by Canetti, Goldreich, Goldwasser, Micali

Assumption: each verifier must be associated with a **permanent** public key, registered **before** any proof starts.

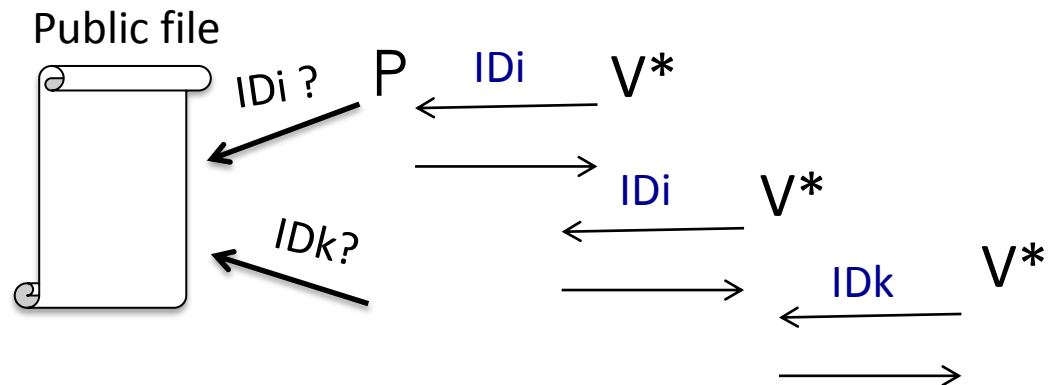
Registration Phase

- Non-interactive
- Fully controlled by V^*
- No trusted party involved

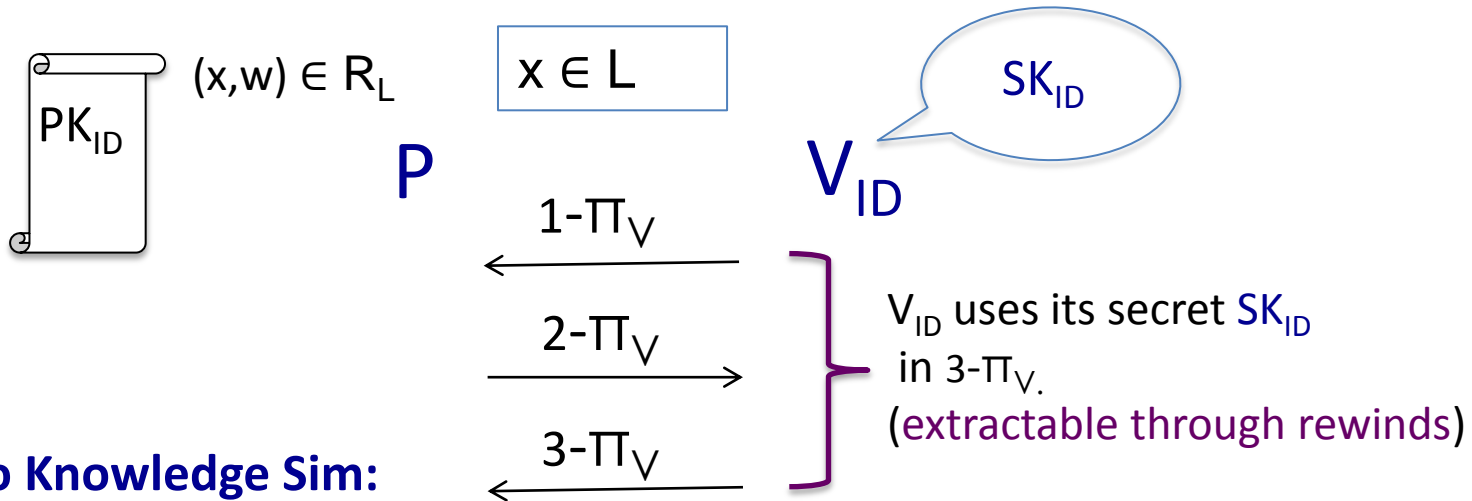


Proof Phase

- V^* can still open an *unbounded* (poly) number of sessions.
- V^* has full control of the schedule
- **Restriction:** V^* cannot play with identity not in public file.

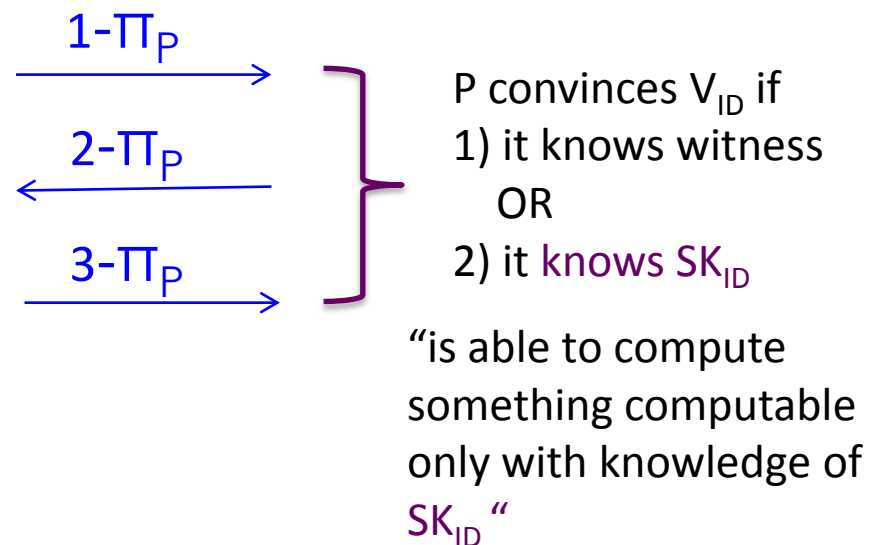


Achieving constant-round concurrent ZK in the BPK model



Concurrent Zero Knowledge Sim:

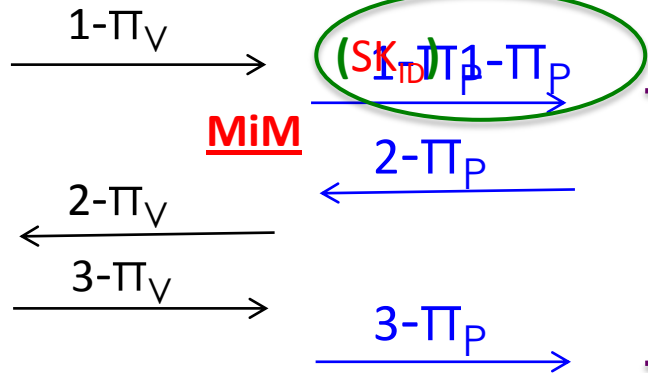
- gets SK_{ID} by rewinding π_V
- runs π_P in straight-line using SK_{ID}
- once SK_{ID} is extracted, all sessions played with V_{ID} are run in straight-line
- **poly**: number of extraction bounded by number of identities.



Concurrent Soundness in the BPK model

IDEA: if known, the secret SK_{ID} should be used *already* in the first msg $1-\pi_P$.

Concurrent executions



MiM

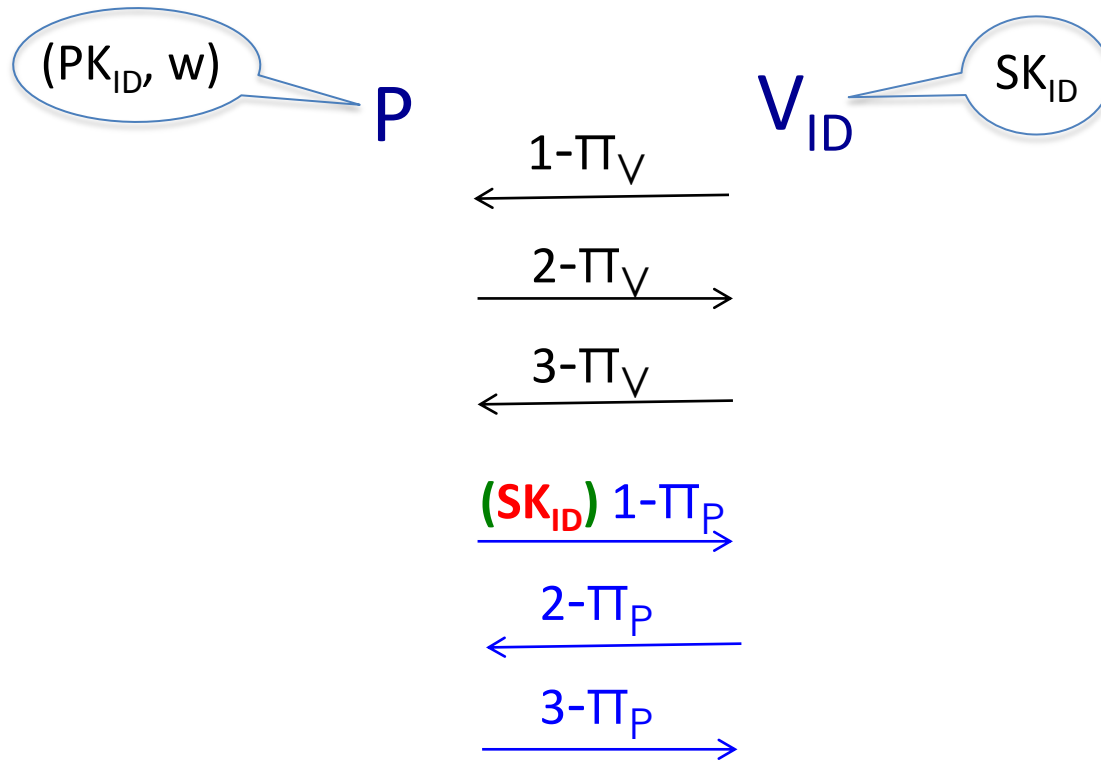
Proving concurrent soundness: rule out MiM Attack

P convinces V_{ID} if
 1) it knows witness
 OR
 2) **it knows SK_{ID}**

Concurrent Zero Knowledge

Still preserved. Sim extracts the secret before having to play the first msg $1-\pi_P$.

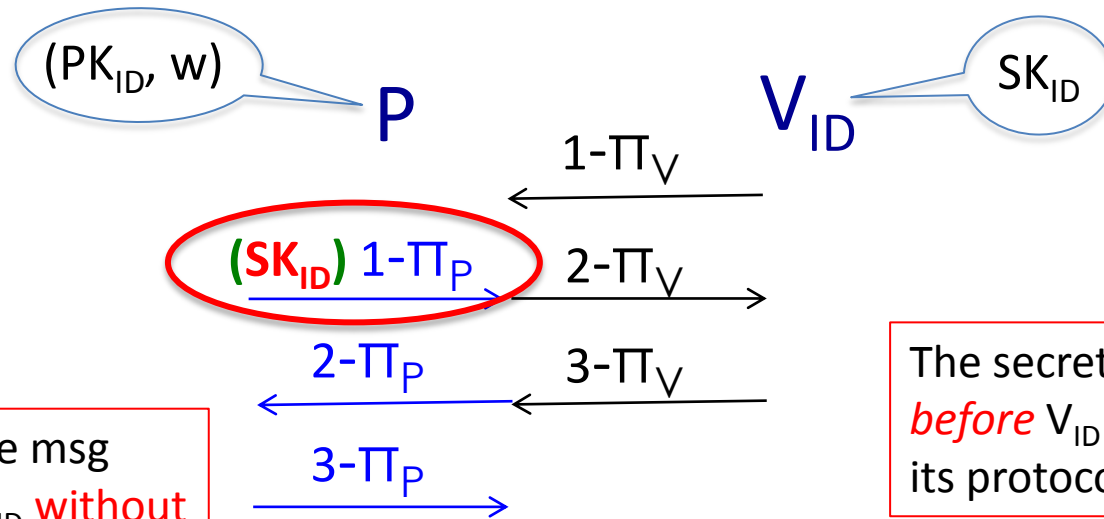
Concurrent Zero Knowledge and Soundness



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Round-Optimal (4 rounds) Concurrent Zero Knowledge and Soundness



Sim has to play the msg dependent on SK_{ID} **without knowing it yet.**

The secret is used **before** V_{ID} completes its protocol.

Concurrent Simulator?

Concurrent Simulator in Literature

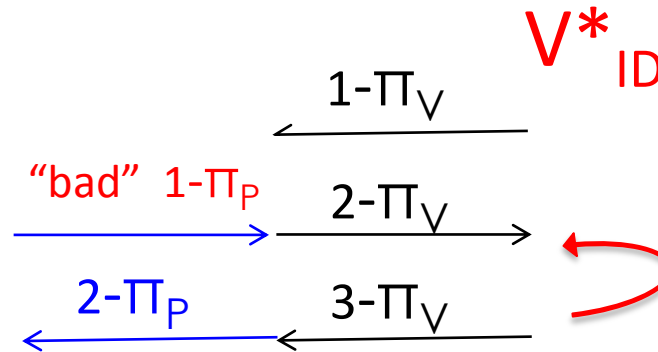
all (*published*) simulators follow this strategy.

Simulation in phases

When playing with an “unresolved” identity:

Sim

1) Play a “bad” first message



2) Extract the secret needed to solve the session.

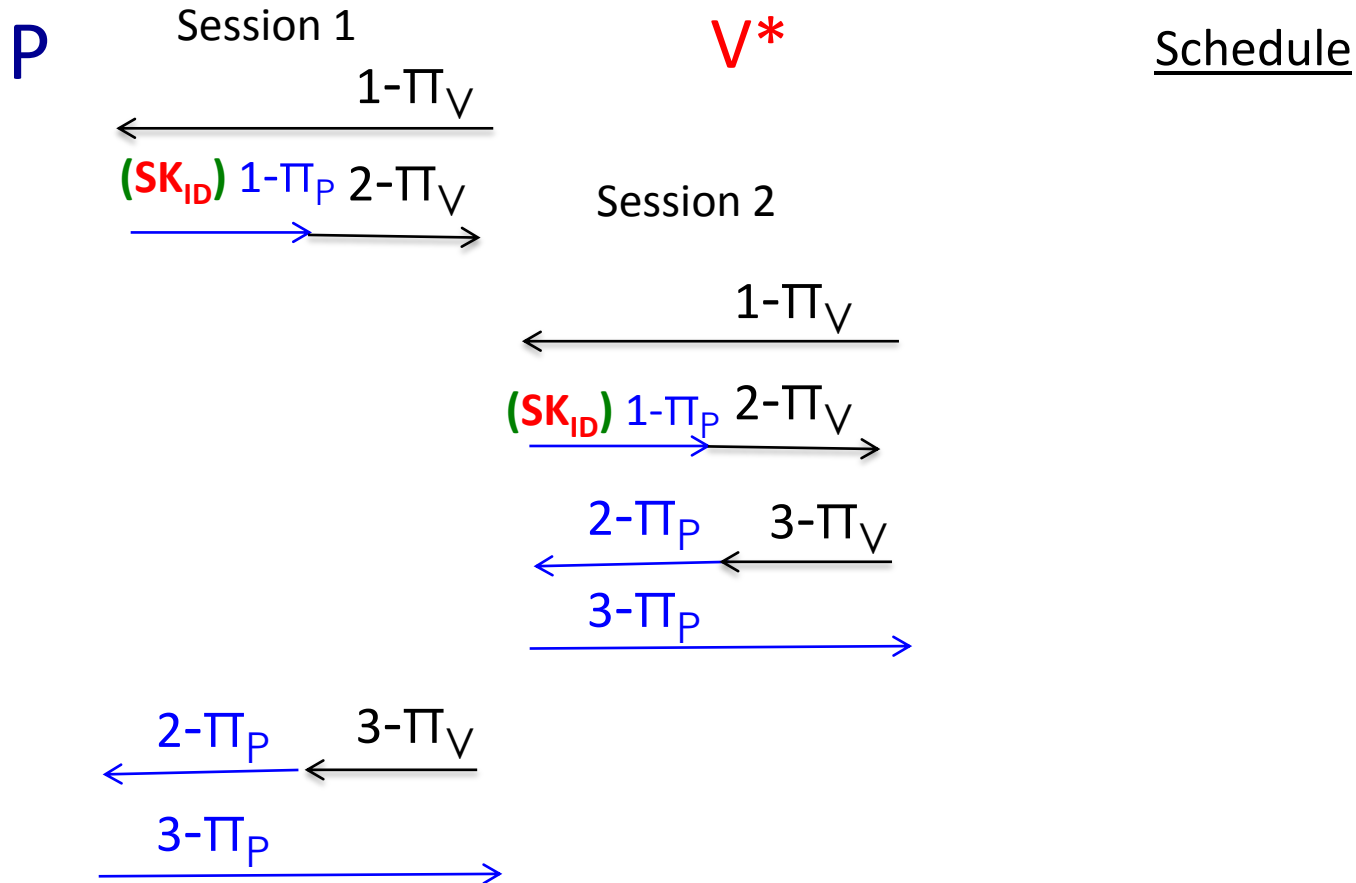
3) Start simulation *from scratch* (a new phase) with knowledge of one more secret SK_{ID} .

Number of phases = number of identities (poly)

Our contribution:

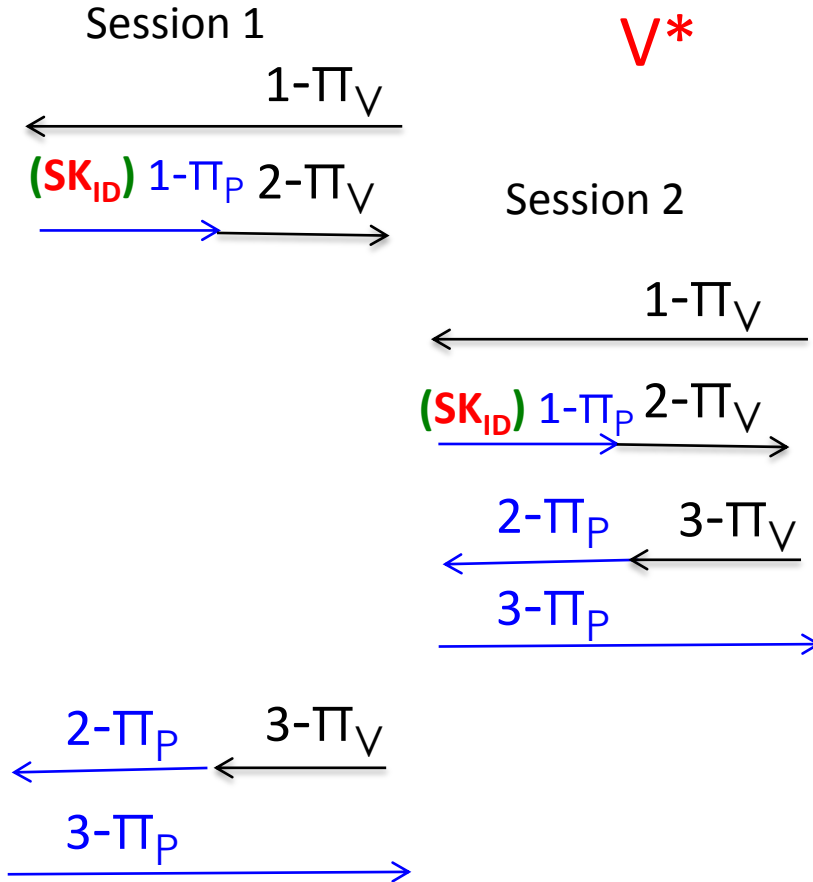
Such simulation approach leads to a **distinguishable distribution.**

A dummy attack



A dummy attack

P



V*

V* Strategy

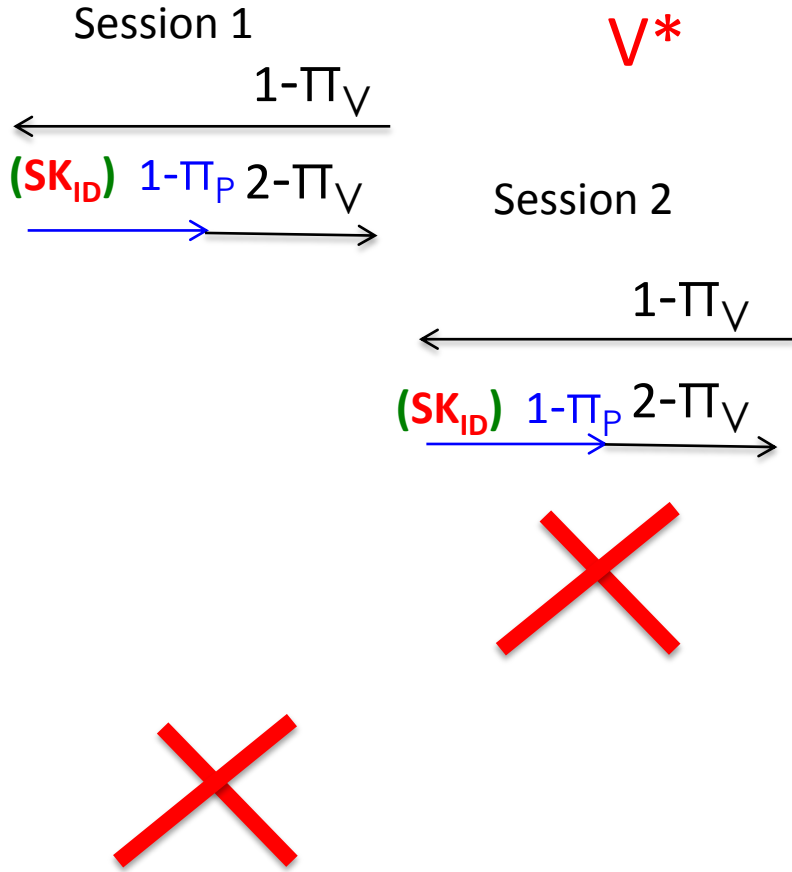
V* aborts Session 1 with prob. 1/2

V* aborts Session 2 with prob. 1/2

(taken over the transcript seen so far)

A dummy attack

P



V^* Strategy

V^* aborts Session 1 with prob. $1/2$

V^* aborts Session 2 with prob. $1/2$

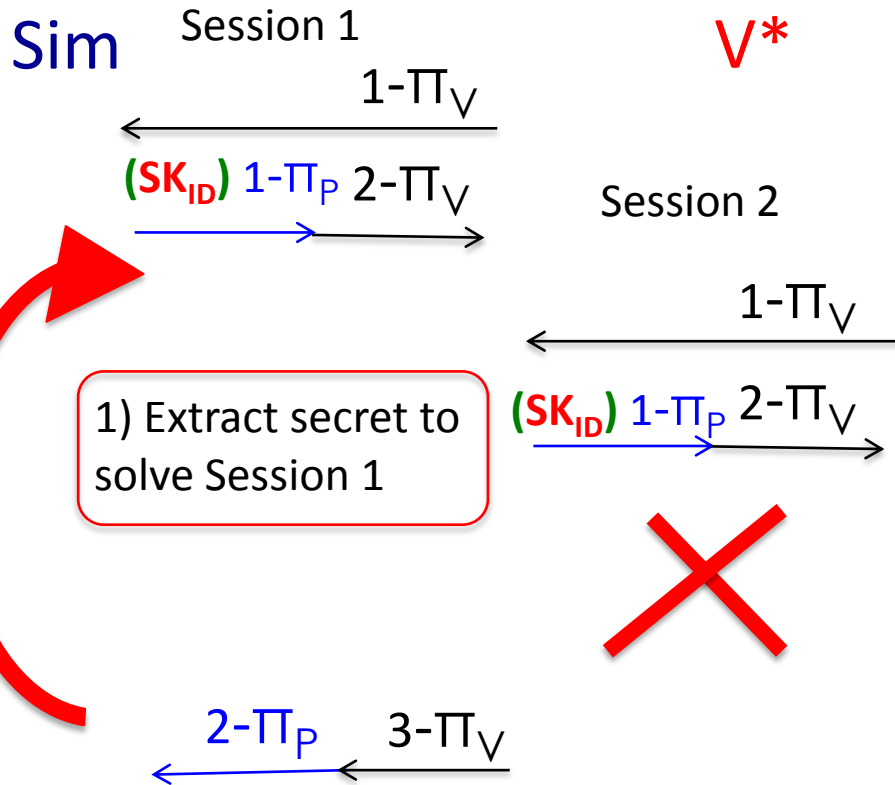
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Prob. Abort in Real Game

$$\Pr[\text{Abort S1}] \times \Pr[\text{Abort S2}] =$$

$$1/2 \times 1/2 = \mathbf{1/4}$$

A dummy attack



V* Strategy

V* aborts Session 1 with prob. $1/2$

V* aborts Session 2 with prob. $1/2$
(taken over the transcript seen so far)

Prob. Abort in Real Game

$$\Pr[\text{Abort S1}] \times \Pr[\text{Abort S2}] = 1/2 \times 1/2 = \mathbf{1/4}$$

Prob. Abort Simulation

Case 1.

$$\Pr[\text{Abort S1}] \times \Pr[\text{Abort S2}] = 1/2 \times 1/2 = 1/4$$

Case 2.

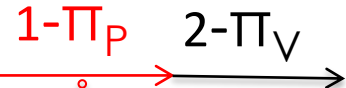
$$\Pr[\text{Abort S2}] \times \Pr[\text{NOT Abort S1}]$$

A dummy attack

2) Start the simulation from scratch with knowledge of secret.

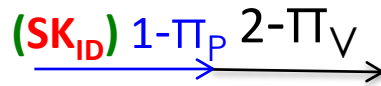
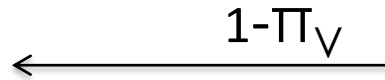
Sim

Session 1



V^*

Session 2



V^* Strategy

V^* aborts Session 1 with prob. $1/2$

V^* aborts Session 2 with prob. $1/2$

(taken over the transcript seen so far)

Prob. Abort in Real Game

$$\Pr[\text{Abort S1}] \times \Pr[\text{Abort S2}] =$$

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Prob. Abort Simulation

Case 1.

$$\Pr[\text{Abort S1}] \times \Pr[\text{Abort S2}] =$$

$$1/2 \times 1/2 = 1/4$$

Case 2.

$$\Pr[\text{Abort S2}] \times \Pr[\text{NOT Abort S1}] \times \Pr[\text{Case 1}]$$

$$= 1/2 \times 1/2 \times \mathbf{1/4} = 1/16$$

Sim outputs two aborts with probability at least

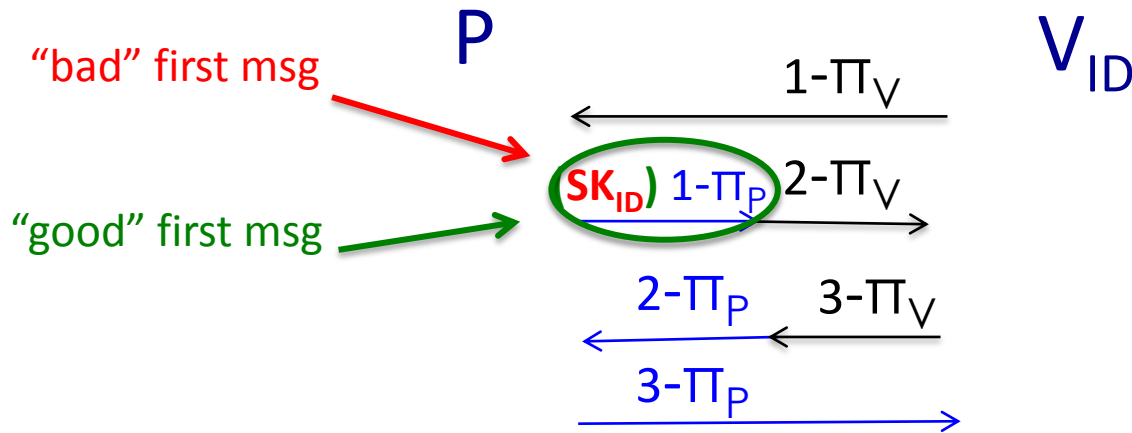
Case 1 + Case 2 > Real Game

Simulation in phases yields a distinguishable output.

Alternative Simulation Strategies?

- Trivially, there exists a simulator for the dummy V^* seen so far.
- what about more sophisticated V^* that aborts with different probability in different sessions....?

The problem: the protocol's structure of *round-optimal* protocols



Remark

Protocols that do not follow this structure could admit alternative strategies:

- resZK [YZ07] complexity leveraging.
- cZK [Z03]: only sequential soundness.

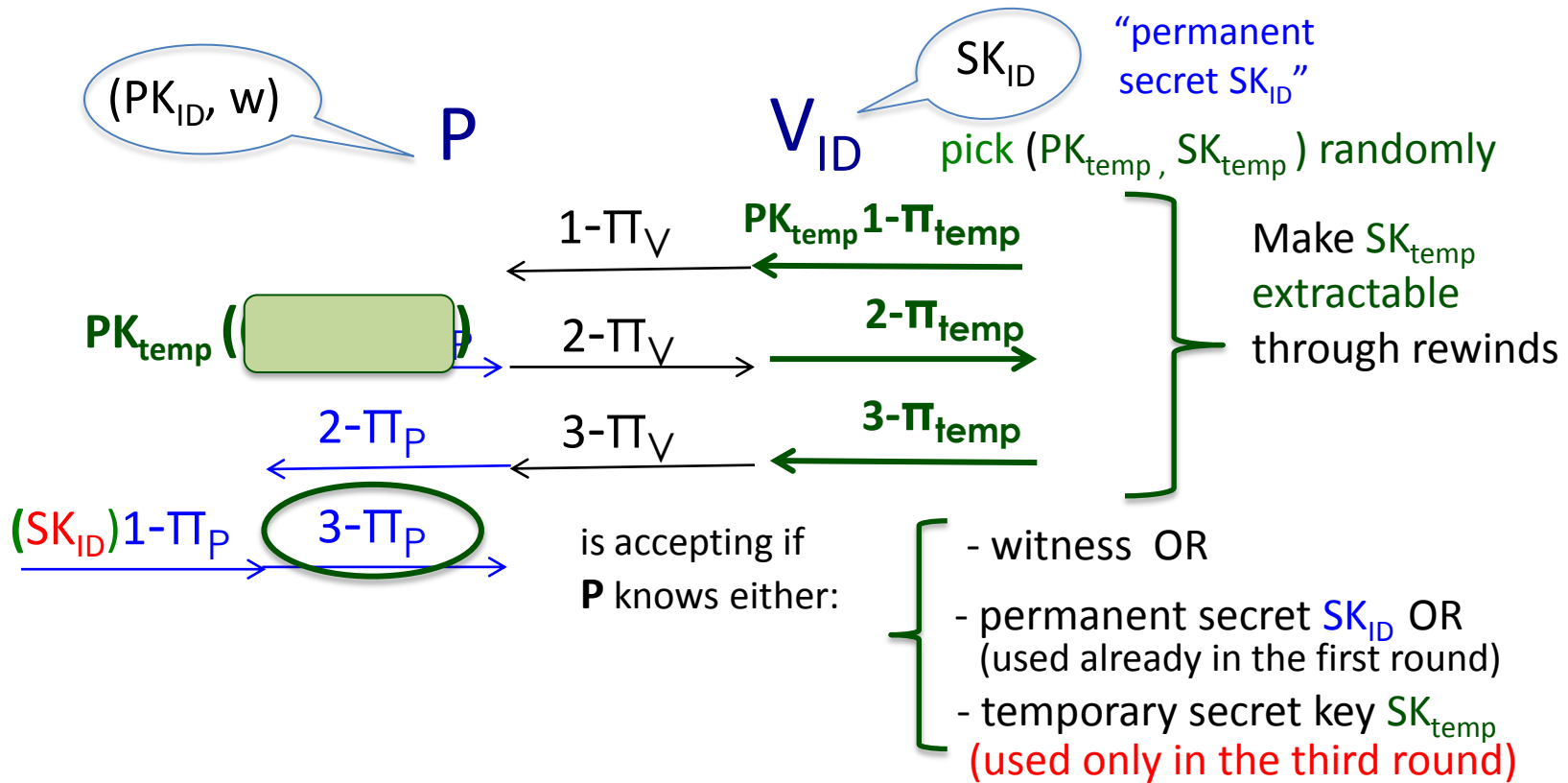
- In order to "solve" a session (played with a new identity) Sim **has to change the view** of the verifier (first play a bad msg, then a good msg)
- changing the view of V^* skews the output distribution.

designing a successful simulation strategy seems problematic.

Outline

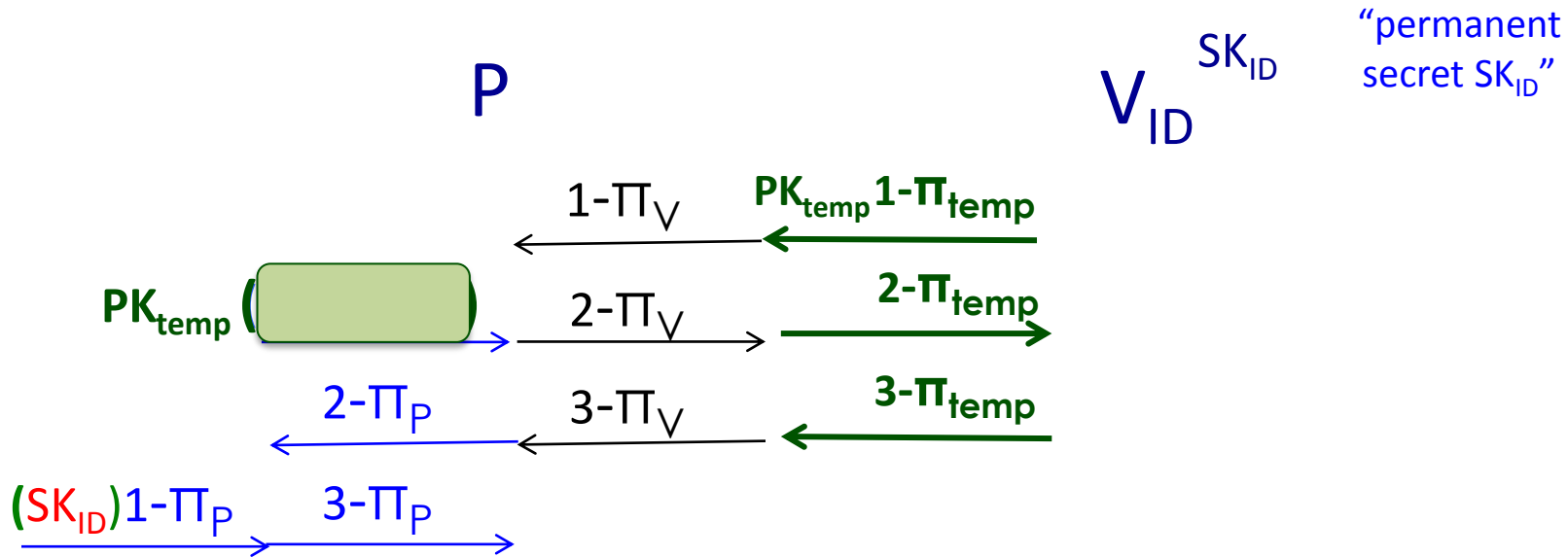
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Our round-optimal concurrent ZK



KEY IDEA. Temporary secret key SK_{temp} is used **only in the last msg** 3- Π_P . (only after the extraction)

The simulator



Two-mode simulation (allows to keep the main thread unchanged)

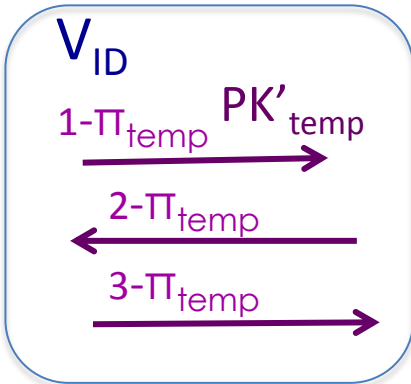
- to solve a session initiated by an unknown identity Sim extracts both permanent SK_{ID} and temporary key SK_{temp} , and computes the last msg using SK_{temp} .
- to solve a session initiated by a known identity Sim runs in straight-line computing $3-\Pi_P$ using the permanent secret SK_{ID} .
- the view of V^* in the two modes must be statistically indistinguishable.

Concurrent soundness?

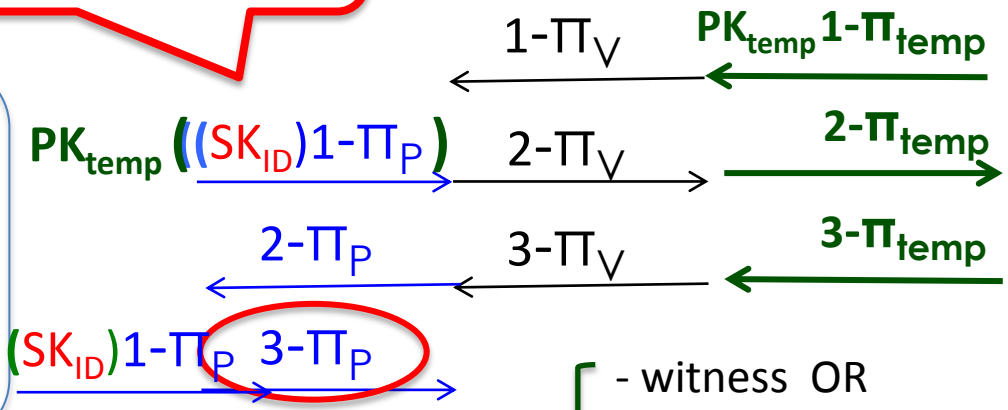
to prove *concurrent soundness* secret must be used **already** in the first msg.

P^*

$V_{ID}^{SK_{ID}}$



Concurrent executions?

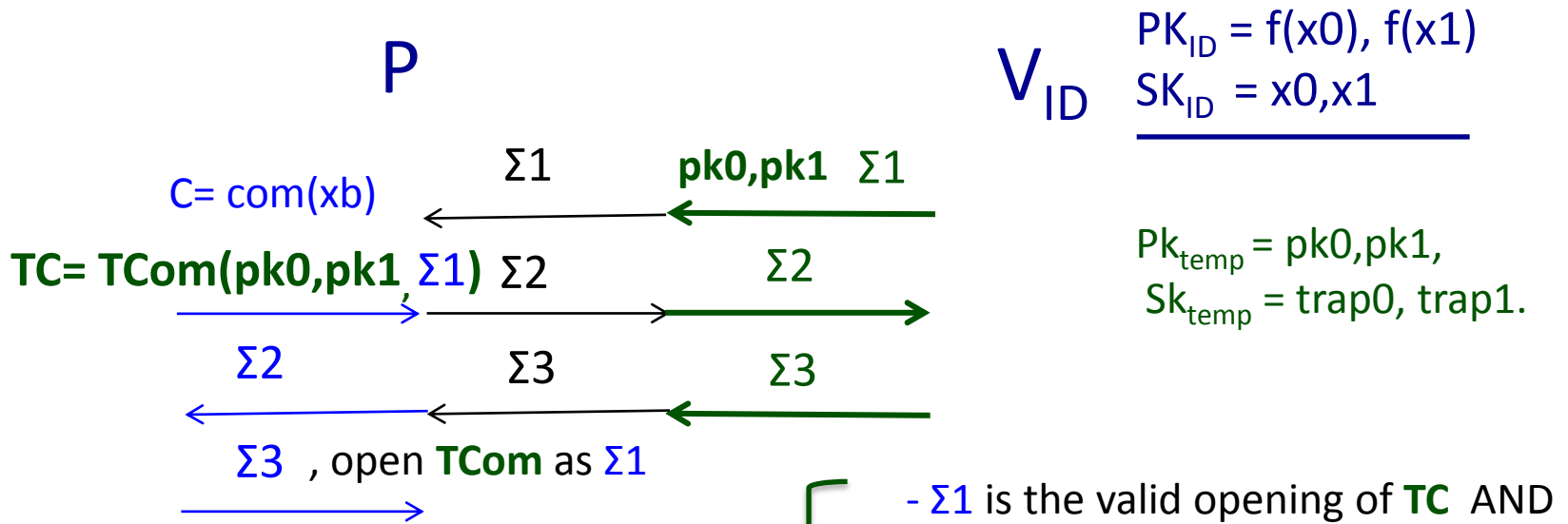


Proof by witness extraction

- witness OR
- permanent secret SK_{ID} OR
- temporary secret key SK_{temp} (used only in the third round)

key point: the temporary keys used in concurrent sessions are *independent*.

Actual implementation



V_{ID}

$PK_{ID} = f(x0), f(x1)$

$SK_{ID} = x0, x1$

$PK_{temp} = pk0, pk1,$

$SK_{temp} = trap0, trap1.$

- $\Pi_V \Pi_{temp} \Pi_P$ are implemented with **Sigma Protocols**.
- **TCom** is a two-round trapdoor commitment scheme.
- f is a OWP.

thanks